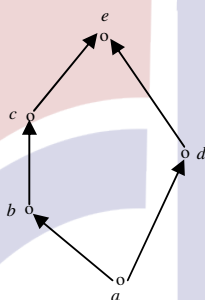


Computer Science and Information Technology

Q. No. 1 – 25 Carry One Mark Each

1. Consider the set $X = \{a, b, c, d, e\}$ under the partial ordering
 $R = \{(a, a), (a, b), (a, c), (a, d), (a, e), (b, b), (b, c), (b, e), (c, c), (c, e), (d, d), (d, e), (e, e)\}$.
 The Hasse diagram of the partial order (X, R) is shown below.



The minimum number of ordered pairs that need to be added to R to make (X, R) a lattice is _____.

Key: (0)

Exp: Given POSET is already a lattice so no need to add any ordered pairs.

2. Which of the following statements about parser is/are CORRECT?
 I. Canonical LR is more powerful than SLR.
 II. SLR is more powerful than LALR
 III. SLR is more powerful than Canonical LR.
 (A) I only (B) II only (C) III only (D) II and III only

Key: (A)

Exp: Bottom up parsers in decreasing order of their power: $CLR \gg LALR \gg SLR \gg LR$ (0)

The given statements:

- I. Canonical LR is more powerful than SLR is **CORRECT**.
 II. SLR is more powerful than LALR is **INCORRECT**
 III. SLR is more powerful than Canonical LR is **INCORRECT**.

3. Match the following:

| | | | |
|-----------|------------------------------|-------------|--|
| P. | static char var; | i. | Sequence of memory locations to store addresses |
| Q. | m= malloc (10); m = NULL; | ii. | A variable located in data section of memory |
| R. | char * ptr [10] | iii. | Request to allocate a CPU register to store data |
| S. | register int var1; | iv. | A lost memory which cannot be freed |

□

- (A) P-(ii), Q-(iv), R-(i), S-(iii) (B) P-(ii), Q-(i), R-(iv), S-(iii)
 (C) P-(ii), Q-(iv), R-(iii), S-(i) (D) P-(iii), Q-(iv), R-(i), S-(ii)

Key: (A)

Exp: P. static char var:

var is defined as character variable whose associated storage class is static because of this it is given memory from data segment .

Q. `m = malloc(10);`

`m = NULL;`

10 contiguous bytes of memory is allocated is address of first byte is stored in 'm' and later it is updated with NULL. Now we lost the address of first bytes of that chunk of memory completely. So we can't free that space as we need the address of first byte to free it up

R. char * ptr [10]:

ptr is an array of 10 pointers pointing to character variables.

S. register int var1:

Suggesting the compiler to store the var1 "value" in CPU register.

4. Let L_1, L_2 be any two context free languages and R be any regular language. Then which of the following is/are CORRECT ?

- I. $L_1 \cup L_2$ is context – free II. $\overline{L_1}$ is context – free
 III. $L_1 - R$ is context – free IV. $L_1 \cap L_2$ is context – free
 (A) I, II and IV only (B) I and III only
 (C) II and IV only (D) I only

Key: (B)

Exp: Given L_1 and L_2 are context free languages and R is a regular language.

- I. $L_1 \cup L_2$ is context free is **CORRECT**, context free language are closed under union operation.
 II. $\overline{L_1}$ is context free is **INCORRECT**, context free languages are not closed under complement operation.
 III. $L_1 - R$ is Context free is **CORRECT**.
 $L_1 - R = L_1 \cap \overline{R}$, Context free intersection Regular is always Context free.
 IV. $L_1 \cap L_2$ is context free is **INCORRECT**; context free languages are not closed under complement operation.

5. G is undirected graph with n vertices and 25 edges such that each vertex of G has degree at least 3. Then the maximum possible value of n is _____.

Key: (16)

Exp: If every vertex has degree at least k then □

$$K|V| \leq 2(E)$$

$$3V \geq 2E$$

$$|V| \leq \left\lfloor \frac{50}{3} \right\rfloor$$

$$|V| \leq 16$$

6. Let p, q, r denote the statements “It is raining”, “It is cold”, and “It is pleasant,” respectively. Then the statement “It is not raining and it is pleasant, and it is not pleasant only if it is raining and it is cold” is represented by

- (A) $(\neg p \wedge r) \wedge (\neg r \rightarrow (p \wedge q))$ (B) $(\neg p \wedge r) \wedge ((p \wedge q) \rightarrow \neg r)$
 (C) $(\neg p \wedge r) \vee ((p \wedge q) \rightarrow \neg r)$ (D) $(\neg p \wedge r) \vee (r \rightarrow (p \wedge q))$

Key: (A)

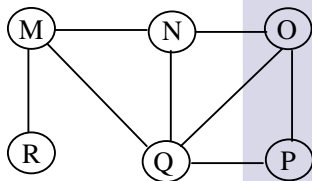
Exp: X only if Y is same as $X \Rightarrow Y$

“it is not raining and it is pleasant” = $\neg p \wedge r$

“it is not pleasant only if it is raining and it is cold” = $\neg r \rightarrow (p \wedge q)$

$$\therefore (\neg p \wedge r) \wedge (\neg r \rightarrow (p \wedge q))$$

7. The Breadth First Search (BFS) algorithm has been implemented using the queue data structure. Which one of the following is a possible order of visiting the nodes in the graph below?



- (A) MNOPQR (B) NQMPOR (C) QMNROP (D) POQNMR

Key: (D)

Exp: **BFS:** Start at root (some arbitrary node of a graph, sometimes referred to as “search key”) and explore the neighbor nodes first, before moving to the next level neighbors.

8. Let $P = \begin{bmatrix} 1 & 1 & -1 \\ 2 & -3 & 4 \\ 3 & -2 & 3 \end{bmatrix}$ and $Q = \begin{bmatrix} -1 & -2 & -1 \\ 6 & 12 & 6 \\ 5 & 10 & 5 \end{bmatrix}$ be two matrices.

Then the rank of $P + Q$ is _____.

□

Key: (2)

Exp:

$$P+Q = \begin{bmatrix} 0 & -1 & 12 \\ 8 & 9 & 10 \\ 8 & 8 & 8 \end{bmatrix}$$

$$R_1 \leftrightarrow R_2 \sim \begin{bmatrix} 8 & 9 & 10 \\ 0 & -1 & -2 \\ 1 & 1 & 1 \end{bmatrix}$$

$$\frac{R_3}{8}$$

$$8R_3 - R_1 \sim \begin{bmatrix} 8 & -9 & 10 \\ 0 & -1 & -2 \\ 0 & -1 & -2 \end{bmatrix}$$

$$R_3 - R_2 \sim \begin{bmatrix} 8 & -9 & 10 \\ 0 & -1 & -2 \\ 0 & 0 & 0 \end{bmatrix}$$

\therefore Rank is 2

9. Consider socket API on a Linux machine that supports connected UDP sockets. A connected UDP socket is a UDP socket on which **connect** function has already been called. Which of the following statements is/are CORRECT ?

- I. A connected UDP socket can be used to communicate with multiple peers simultaneously.
 II. A process can successfully call **connect** function again for an already connected UDP socket.

(A) I only (B) II only (C) Both I and II (D) Neither I nor IIs

Key: (B)

Exp: A process with a connected UDP socket can call connect again for that socket for one of two reasons:

- (1) To specify a new IP address and port.
 (2) To unconnect the socket.

10. The minimum possible number of states of a deterministic automaton that accepts the regular language

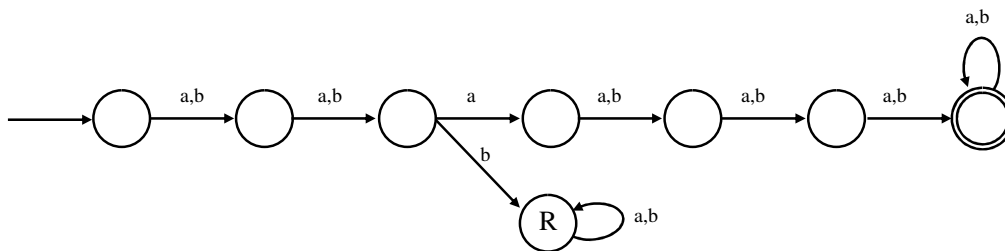
$$L = \{w_1aw_2 \mid w_1, w_2 \in \{a, b\}^*, |w_1| = 2, |w_2| \geq 3\}$$
 is _____.

Key: (8)

Exp: The Given regular language is

$$L = \{w_1aw_2 \mid w_1, w_2 \in \{a, b\}^*, |w_1| = 2 \mid w_2| \geq 3\}$$

The minimal Deterministic finite automata accepting L is: □



11. Consider the following tables T1 and T2.

| P | Q |
|---|---|
| 2 | 2 |
| 3 | 8 |
| 7 | 3 |
| 5 | 8 |
| 6 | 9 |
| 8 | 5 |
| 9 | 8 |

| R | S |
|---|---|
| 2 | 2 |
| 8 | 3 |
| 3 | 2 |
| 9 | 7 |
| 5 | 7 |
| 7 | 2 |

In table T1, **P** is the primary key and **Q** is the foreign key referencing **R** in table T2 with on-delete cascade and on-update cascade. In table T2, **R** is the primary key and **S** is the foreign key referencing **P** in table T1 on-delete set NULL and on-update cascade. In order to delete record $\langle 3,8 \rangle$ from table T1, the number of additional records that need to be deleted from table T1 is _____.

Key: (0)

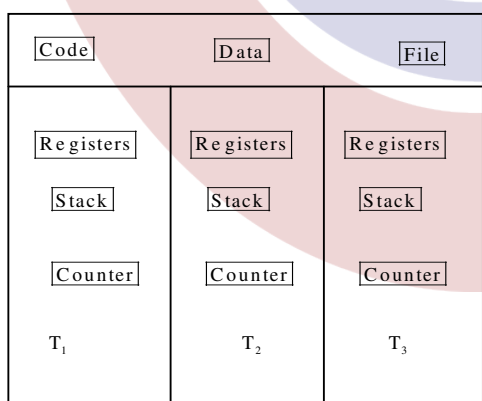
Exp: Only (8,3) will be deleted from T2.

12. Which of the following is/are shared by all the threads in a process ?

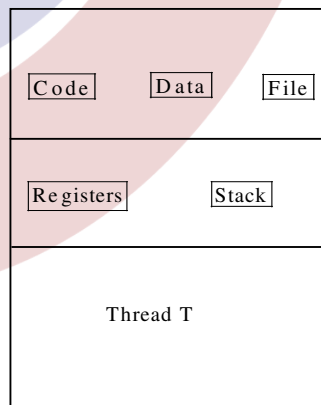
- I. Program counter
 - II. Stack
 - III. Address space
 - IV. Registers
- (A) I and II only (B) III only (C) IV only (D) III and IV only

Key: (B)

Exp:



Single process P with 3 threads Multi threading



Single threaded process

□

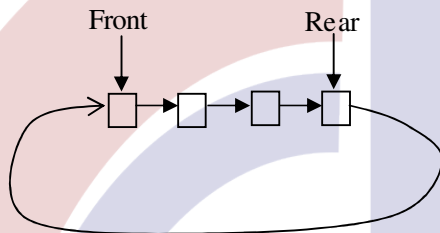
13. A circular queue has been implemented using a single linked list where each node consists of a value and a single pointer pointing to the next node. We maintain exactly two external pointers **FRONT** and **REAR** pointing to the front node and the rear node of the queue, respectively. Which of the following statements is/are **CORRECT** for such a circular queue, so that insertion and deletion operation can be performed in O(1) time ?

- I. Next pointer of front node points to the rear node.
- II. Next pointer of rear node points to the front node.

(A) I only (B) II only (C) Both I and II (D) Neither I nor II

Key: (B)

Exp: Next pointer of the front node would point to the second node, if any.



14. Given the following binary number in 32-bit (single precision) IEEE-754 format:

00111110011011010000000000000000

The decimal value closest to this floating- point number is

- (A) 1.45×10^1
- (B) 1.45×10^{-1}
- (C) 2.27×10^{-1}
- (D) 2.27×10^1

Key: (C)

Exp: Sign

0 01111100

110110100000000000000000

+1 124

+1 2^{-3}

$$[2^{-12} + 2^{-13} + \dots] = 0.227\dots$$

$$[1 +]0.8515625$$

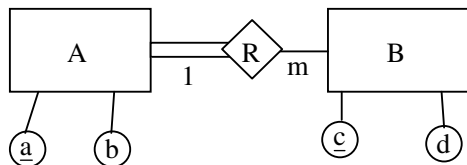
15. An ER model of a database consists of entity types A and B. These are connected by a relationship R which does not have its own attribute. Under which one of the following conditions, can the relational table for R be merged with that of A?

- (A) Relationship R is one-to-many and the participation of A in R is total
- (B) Relationship R is one-to-many and the participation of A in R is partial
- (C) Relationship R is many-to-one and the participation of A in R is total
- (D) Relationship R is many-to-one and the participation of A in R is partial

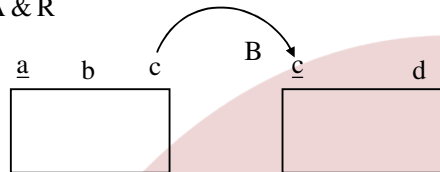
Key: (C)

□

Exp:



A & R



Note: only M ! N relationship needs exclusive table: If a relationship is 1 ! M or M ! 1 then that relation could be included in the many side table with the help of foreign key concept.

16. Match the algorithms with their time complexities:

| Algorithm | | Time complexity | |
|-----------|---|-----------------|--------------------|
| P. | Towers of Hanoi with n disks | i. | $\theta(n^2)$ |
| Q. | Binary search given n sorted numbers | ii. | $\theta(n \log n)$ |
| R. | Heap sort given n numbers at the worst case | iii. | $\theta(2^n)$ |
| S. | Addition of two $n \times n$ matrices | iv. | $\theta(\log n)$ |

- (A) P-(iii),Q-(iv), R-(i), S-(ii) (B) P-(iv),Q-(iii), R-(i), S-(ii)
 (C) P-(iii),Q-(iv), R-(ii), S-(i) (D) P-(iv),Q-(iii), R-(ii), S-(i)

Key: (C)

Exp: P. Towers of Hanoi $\Rightarrow T(n) = 2T(n-1) + 1 \Rightarrow \theta(2^n)$

Q. Binary search $\Rightarrow T(n) = T\left(\frac{n}{2}\right) + C \Rightarrow \theta(\log n)$

R. Heap sort $\Rightarrow \theta(n \log n)$

S. Addition of two $n \times n$ matrices $\Rightarrow \theta(n^2)$

17. Match the following according to input (from the left column) to the compiler phase (in the right column) that processes it.

| Column-1 | | Column-2 | |
|----------|-----------------------------|----------|-------------------|
| P. | Syntax tree | i. | Code generator |
| Q. | Character stream | ii. | Syntax analyzer |
| R. | Intermediate representation | iii. | Semantic analyzer |
| S. | Token stream | iv. | Lexical analyzer |

□

- (A) P-(ii),Q-(iii), R-(iv), S-(i) (B) P-(ii),Q-(i), R-(iii), S-(iv)
 (C) P-(iii),Q-(iv), R-(i), S-(ii) (D) P-(i),Q-(iv), R-(ii), S-(iii)

Key: (C)

Exp: Lexical Analysis phase processes character stream and generates tokens, e.g. identifier or keywords.

Tokens are processed by Syntax analysis analyzer.

Syntax tree is processed by Semantic analyzer.

Intermediate code such as 3-address code is used for code generation process.

18. Consider the following statements about the routing protocols, Routing Information Protocol (RIP) and Open Shortest Path First (OSPF) in an IPv4 network.

- I. RIP uses distance vector routing
 II. RIP packets are sent using UDP
 III. OSPF packets are sent using TCP
 IV. OSPF operation is based on link-state routing

Which of the statements above are CORRECT?

- (A) I and IV only (B) I, II and III only
 (C) I, II and IV only (D) II, III and IV only

Key: (C)

Exp: **Statement (1):** RIP uses distance vector routing. "CORRECT"

RIP is one of the oldest DVR protocol which employ the hop count as a routing metric.

Statement (2): RIP packets are sent using UDP. "CORRECT"

RIP uses the UDP as its transport protocol, and is assigned the reserved port no 520.

Statement (3): OSPF packets are sent using TCP. "INCORRECT"

OSPF does not use a transport protocol, such as UDP (or) TCP, but encapsulates its data directly in IP packets.

Statement (4): OSPF operation is based on link state routing. "CORRECT"

OSPF is a routing protocol which uses link state routing (LSR) and works within a single autonomous system.

Hence Option "C" is correct.

19. If $f(x) = R \sin\left(\frac{\pi x}{2}\right) + S$, $f'\left(\frac{1}{2}\right) = \sqrt{2}$ and $\int_0^1 f(x) dx = \frac{2R}{\pi}$, then the constants R and S are, respectively

- (A) $\frac{2}{\pi}$ and $\frac{16}{\pi}$ (B) $\frac{2}{\pi}$ and 0 (C) $\frac{4}{\pi}$ and 0 (D) $\frac{4}{\pi}$ and $\frac{16}{\pi}$

Key: (C)

Exp: $f'(x) = \frac{R\pi}{2} \cos\left(\frac{\pi x}{2}\right)$ □

$$\Rightarrow f'(1/2) = \sqrt{2} \text{ gives } \frac{R\pi}{2\sqrt{2}} \sqrt{2} \Rightarrow R = \frac{4}{\pi}$$

Also $\int_0^1 f(x) dx = \frac{2R}{\pi}$ gives $\frac{-2R}{\pi} \left(\cos \frac{\pi x}{2} \right)_0^1 + S(x)_0^1 = 2R/\pi$
 $\Rightarrow S=0$

20. In a file allocation system, which of the following allocation schemes(s) can be used if no external fragmentation is allowed?

- I. Contiguous II. Linked III. Indexed
 (A) I and III only (B) II only (C) III only (D) II and III only

Key: (D)

Exp: Contiguous allocation suffer from external fragmentation. But linked and indexed allocation schemes free from external fragmentation. Hence, option D is correct.

21. Consider a quadratic equation $x^2 - 13x + 36 = 0$ with coefficients in a base b. The solutions of this equation in the same base b are $x = 5$ and $x = 6$. Then $b =$ _____.

Key: (8)

Exp: Clearly $13 = 1 \times 10 + 3$ and $36 = 3 \times 10 + 6 \Rightarrow$ base $b = 10$

The quadratic equation with solutions $x = 5$ and $x = 6$ is $x^2 - 11x + 30 = 0$

According to the given condition, we have $b + 3 = 11$ and $3b + 6 = 30 \Rightarrow b = 8$

Answer is 8.

Alternate solution:

$x^2 - 13x + 36 = 0$ (given quadratic equation)

In base b, $13 = 1 \times b^1 + 3 \times b^0 = b + 3$ and

$36 = 3 \times b^1 + 6 \times b^0 = 3b + 6$

So the equation becomes $x^2 - (b + 3)x + (3b + 6) = 0$

Since $x = 5$ is a solution

$\therefore 5^2 - (b + 3)5 + (3b + 6) = 0 \Rightarrow b = 8$

Similarly, by putting $x = 6$, we get $b = 8$

22. Identify the language generated by the following grammar, where S is start variable.

$S \rightarrow XY$

$X \rightarrow aX|a$

$Y \rightarrow aYb|\epsilon$

(A) $\{a^m b^n \mid m \geq n, n > 0\}$ (B) $\{a^m b^n \mid m \geq n, n \geq 0\}$

(C) $\{a^m b^n \mid m > n, n \geq 0\}$ (D) $\{a^m b^n \mid m > n, n > 0\}$

Key: (C)

Exp: The given grammar with S as start symbol is

$S \rightarrow XY$

□

$X \rightarrow aX|a$

$Y \rightarrow aYb|c$

From Non terminal X we can generate any number of a 's including a single ' a ' and from Y equal number of a 's and b 's.

Hence $L = \{a^m b^n | m > n, n \geq 0\}$

23. The representation of the value of a 16-bit unsigned integer X in hexadecimal number system is $BCA9$. The representation of the value of X in octal number system is

(A) 571244 (B) 736251 (C) 571247 (D) 136251

Key: (D)

Exp: $(BCA9)_{16} \rightarrow (136251)_8$

Convert hexadecimal to octal number system.

24. Consider the following function implemented in C:

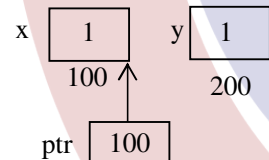
```
void printxy (int x, int y) {
    int *ptr ;
    x = 0;
    ptr = &x;
    y = * ptr;
    * ptr = 1;
    printf ("%d, %d," x, y);
}
```

The output of invoking `printxy (1, 1)` is

(A) 0,0 (B) 0,1 (C) 1,0 (D) 1,1

Key: (C)

Exp:



$\therefore 1,0$ is printed

25. The maximum number of IPv4 router addresses that can be listed in the record route (RR) option field of an IPv4 header is _____.

Key: (9)

Exp: A record route option is used to record the internet routers that handles the datagram. It can list up to nine router addresses. It can be used for debugging and management purpose. □

Q. No. 26 – 55 Carry Two Marks Each

26. Consider a binary code that consists of only four valid code words as given below:

00000,01011,10101,11110

Let the minimum Hamming distance of the code be p and the maximum number of erroneous bits that can be corrected by the code be q . Then the values of p and q are

- (A) $p = 3$ and $q = 1$ (B) $p = 3$ and $q = 2$
 (C) $p = 4$ and $q = 1$ (D) $p = 4$ and $q = 2$

Key: (A)

Exp: Given :

code1 00000

code2 01011

code3 10101

code4 11110

Hamming distance between code 1 and code 2 is 3.

Hamming distance between code 1 and code 3 is 3.

Hamming distance between code 1 and code 4 is 4.

Hamming distance between code 2 and code 3 is 4.

Hamming distance between code 2 and code 4 is 3.

Hamming distance between code 3 and code 4 is 3.

So, as per Hamming code, minimum Hamming distance of all code words is considered as Hamming distance i.e., 3 (p).

Now, the max number of erroneous bits that can be corrected by the Hamming code is $2d + 1$.

So,

$$2d + 1 = 3 \Rightarrow d = 1$$

So option A is correct.

27. A system shares 9 tape drives. The current allocation and maximum requirement of tape drives for three processes are shown below:

| Process | Current Allocation | Maximum Requirement |
|---------|--------------------|---------------------|
| P1 | 3 | 7 |
| P2 | 1 | 6 |
| P3 | 3 | 5 |

Which of the following best describes current state of the system ?

- (A) Safe, Deadlocked (B) Safe, Not Deadlocked
 (C) Not Safe, Deadlocked (D) Not Safe, Not deadlocked

Key: (B)

Exp:

| PID | Current Allocation | Max need | Available | Need |
|----------------|--------------------|----------|-----------|------|
| P ₁ | 3 | 3 | 2 | 4 |
| P ₂ | 1 | 6 | - | 5 |
| P ₃ | 3 | 5 | - | 2 |

With the above state of systems, we can get the following 2 safe sequences.

(1) < P₃, P₂, P₁ >

(2) < P₃, P₁, P₂ >

Hence, system is in safe state, no deadlocked option B is correct.

28. Two transactions T₁ and T₂ are given as:

T₁ : r₁(X) w₁(X) r₁(Y) w₁(Y)

T₂ : r₂(Y) w₂(Y) r₂(Z) w₂(Z)

where r_i(V) denotes a read operation by transaction T_i on a variable V and w_i(V) denotes a write operations by transaction T_i on a variable V. The total number of conflict serializable schedules that can be formed by T₁ and T₂ is _____.

Key: (54)

Exp: Conflict conditions RW WR WW

∴ 5 conflicts

| | | | |
|---------------------------------|--------------------|--------------------|--------------------|
| T ₁ - T ₂ | | | |
| a | b | c | d |
| r ₁ (X) | w ₁ (X) | r ₁ (Y) | w ₁ (Y) |
| r ₂ (Y) | w ₂ (Y) | r ₂ (Z) | w ₂ (Z) |
| 1 | 2 | 3 | 4 |

Constraints:

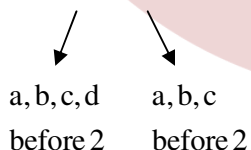
a < b < c < d

1 < 2 < 3 < 4

d < 1 (or) 2 < c

only 1 way

Total = 70 = 70 - (12 + 5)



Therefore, 53 + 1 = 54

□

29. If w, x, y, z are Boolean variables, then which one of the following is INCORRECT ?
- (A) $wx + w(x + y) + x(x + y) = x + wy$
- (B) $\overline{wx}(y + \overline{z}) + \overline{wx} = \overline{w} + x + \overline{yz}$
- (C) $(w\overline{x}(y + x\overline{z}) + \overline{wx})y = x\overline{y}$
- (D) $(w + y)(wxy + wyz) = wxy + wyz$

Key: (C)

Exp:

(A) LHS: $wx + w(x + y) + x(x + y) = x + wy$

RHS:

$$\Rightarrow wx + wx + wy + xx + xy$$

$$\Rightarrow wx + wy + x + xy \quad [\because xx = x]$$

$$\Rightarrow x[1 + y + w] + wy \quad [\because 1 + x = 1]$$

$$\Rightarrow x + wy$$

$$\Rightarrow \text{L.H.S} = \text{R.H.S}$$

(B) L.H.S: $\overline{wx}(y + \overline{z}) + \overline{wx} = \overline{wx} + \overline{yz}$

R.H.S: $\overline{wx}(y + \overline{z}) + \overline{wx}$

Apply De'Morgan theorem

$$\Rightarrow \overline{wx} + (\overline{y + \overline{z}}) + \overline{wx} [\overline{x + y} = \overline{x} \cdot \overline{y}]$$

$$\Rightarrow (\overline{w} + \overline{x}) + (\overline{yz}) + \overline{wx}$$

$$\Rightarrow \overline{w} + \overline{x} + \overline{yz} + \overline{wx}$$

$$\Rightarrow \overline{w} + \overline{x} + \overline{yz} = \text{R.H.S}$$

$$\text{L.H.S} = \text{R.H.S}$$

(C) $\{ \overline{wx}(y + \overline{z}) + \overline{wx} \} y = x\overline{y}$

$$\text{L.H.S} \neq \text{R.H.S}$$

(D) L.H.S: $(w + y)(wxy + wyz) = wxy + wyz$

$$(w + y)(wxy + wyz)$$

$$\Rightarrow wxy + wyz + wxy + wyz$$

$$\Rightarrow wxy + wyz$$

$$\text{L.H.S} = \text{R.H.S}$$

□

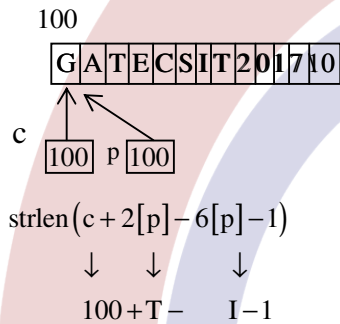
30. Consider the following C Program.

```
#include <stdio.h>
#include <string.h>
int main () {
    char* c = "GATECSIT2017";
    char* p = c;
    printf("%d", (int) strlen (c+2[p]-6[p]-1));
    return 0;
}
```

The output of the program is _____.

Key: (2)

Exp:



Note: Whenever we have characters in the arithmetic expressions, we can replace those with their ASCII values

$\text{Strlen}(100 + x + 11 - x - 1)$ [assume x has the ASCII value of I]
 $\Rightarrow \text{Strlen}(110)$
 $\therefore 2$ is printed

31. P and Q are considering to apply for a job. The probability that P applies for the job is $\frac{1}{4}$. The probability that P applies for the job given that Q applies for the job is $\frac{1}{2}$, and the probability that Q applies for the job given that P applies for the job is $\frac{1}{3}$. Then the probability that P does not apply for the job given that Q does not apply for the job is

- (A) $\frac{4}{5}$ (B) $\frac{5}{6}$ (C) $\frac{7}{8}$ (D) $\frac{11}{12}$

Key: (A)

Exp: Let A,B be the events denote that P, Q respectively applies for a job

$\Rightarrow \text{Pr}(A) = \frac{1}{4}, \text{Pr}(A/B) = \frac{1}{2} \dots (1)$ and $\text{Pr}(B/A) = \frac{1}{3} \dots (2)$ □

(2) gives $\text{Pr}(A \cap B) = \frac{1}{12}$

$$\therefore (1) \text{ gives } Pr(B) = \frac{1}{6}$$

$$\therefore Pr\left(\frac{\bar{A}}{B}\right) = \frac{Pr(\bar{A} \cap \bar{B})}{Pr(\bar{B})} = \frac{1 - Pr(A \cup B)}{1 - Pr(B)} = \frac{1 - \left(\frac{1}{4} + \frac{1}{6} - \frac{1}{12}\right)}{1 - \frac{1}{6}} = \frac{2}{3} \times \frac{6}{5} = \frac{4}{5}$$

$$\left(\text{Here Pr is Probability and } P(A/B) = \frac{P(A \cap B)}{P(B)} \right)$$

32. If the characteristics polynomial of 3×3 matrix M over R (the set of real numbers) is $\lambda^3 - 4\lambda^2 + a\lambda + 30, a \in R$, and one eigenvalue of M is 2, then the largest among the absolute values of the eigenvalues of M is _____.

Key: (5)

Exp: $E(X) = 5 \Rightarrow (X^2) = 30$, where $X \sim P(\lambda), \lambda = 5$

$$\therefore E[(X+2)^2] = E(X^2) + 4E(X) + 4 = 30 + 20 + 4 = 54$$

$$(\because V(X) = E(X^2) - (E(X))^2)$$

Since one eigen value of M is 2

$$\therefore 2^3 - 4(2)^2 + a(2) + 30 = 0$$

$$\Rightarrow a = -11$$

\therefore Characteristic polynomial is

$$\lambda^3 - 4\lambda^2 - 11\lambda + 30 = 0$$

$$(\lambda - 2)(\lambda - 5)(\lambda + 3) = 0$$

$$\therefore \lambda = 2, 5, -3$$

Largest absolute value of ' λ ' is 5

33. Consider the following expression grammar G :

$$E \rightarrow E - T \mid T$$

$$T \rightarrow T + F \mid F$$

$$F \rightarrow (E) \mid id$$

Which of the following grammars is not left recursive, but is equivalent to G ?

(A) $E \rightarrow E - T \mid T$

$$T \rightarrow T + F \mid F$$

$$F \rightarrow (E) \mid id$$

(B) $E \rightarrow TE'$

$$E' \rightarrow -TE' \mid \epsilon$$

$$T \rightarrow T + F \mid F$$

$$F \rightarrow (E) \mid id$$

□

- (C) $E \rightarrow TX$
 $X \rightarrow -TX\epsilon$
 $T \rightarrow FY$
 $Y \rightarrow +FY\epsilon$
 $F \rightarrow (E) \mid id$
- (D) $E \rightarrow TX \mid (TX)$
 $X \rightarrow -TX \mid +TX\epsilon$
 $T \rightarrow id$

Key: (C)

Exp: The rule for removal of left recursion is

$A \rightarrow A\alpha \mid \beta$ will be

$A \rightarrow \beta A'$

$A' \rightarrow \alpha A' \mid \epsilon$

The given grammar is:

$E \rightarrow E - T \mid T$; in this α is “- T” and β is T

$T \rightarrow T + F \mid F$, In this α is “+ F” and β is F

$F \rightarrow (E) \mid id$

Hence after removal of the left recursion:

$E \rightarrow TX$

$X \rightarrow -TX \mid \epsilon$

$T \rightarrow FY$

$Y \rightarrow +FY \mid \epsilon$

$F \rightarrow (E) \mid id$

34. In a two-level cache system, the access times of L_1 and L_2 caches are 1 and 8 clock cycles, respectively. The miss penalty from L_2 cache to main memory is 18 clock cycles. The miss rate of L_1 cache is twice that of L_2 . The average memory access time (AMAT) of this cache system is 2 cycles. This miss rates of L_1 and L_2 respectively are :
- (A) 0.111 and 0.056 (B) 0.056 and 0.111
 (C) 0.0892 and 0.1784 (D) 0.1784 and 0.0892

Key: (A)

Exp: $2 = 1 + 2m \times 8 + m \times 18$

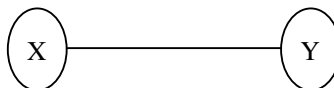
$$\therefore m = \frac{1}{34}$$

35. Consider two hosts X and Y, connected by a single direct link of rate 10^6 bits/sec. The distance between the two hosts is 10,000 km and the propagation speed along the link is 2×10^8 m/sec. Host X sends a file of 50,000 bytes as one large message to host Y continuously. Let the transmission and propagation delays be p milliseconds and q milliseconds, respectively. Then the values of p and q are
- (A) $p = 50$ and $q = 100$ (B) $p = 50$ and $q = 400$ □
 (C) $p = 100$ and $q = 50$ (D) $p = 400$ and $q = 50$

Key: (D)

Exp: Given data

$B = 10^6 \text{ bits / sec}$
 $d = 10,000 \text{ km} = 10^4 \times 10^3 \text{ m}$
 $V = 2 \times 10^8 \text{ m / s}$
 $L = 50,000 \text{ Bytes}$



∴ Transmission time (p) = $\frac{L}{B} = \frac{50,000 \times 8}{10^6} = 400 \text{ ms}$

□ Propagation Time (q) = $\frac{d}{v} = \frac{10^7}{2 \times 10^8} = 50 \text{ ms}$

36. Consider the recurrence function

$$T(n) = \begin{cases} 2T(\sqrt{n}) + 1, & n > 2 \\ 2, & 0 < n \leq 2 \end{cases}$$

Then T(n) in terms of θ notation is

- (A) $\theta(\log \log n)$ (B) $\theta(\log n)$ (C) $\theta(\sqrt{n})$ (D) $\theta(n)$

Key: (B)

Exp: $T(n) = 2T(\sqrt{n}) + 1$
 Put $n = 2^k$
 $T(2^k) = 2T(2^{k/2}) + 1$
 Assume $T(2^k) = \delta(k)$
 $\Rightarrow \delta(k) = 2\delta\left(\frac{k}{2}\right) + 1$

By master's theorem

$\delta(k) = \theta(k)$
 $T(2^k) = \theta(k)$
 $T(n) = \theta(\log n) \quad \because 2^k = n$

37. If a random variable X has a Poisson distribution with mean 5, then the expectation

$E[(X+2)^2]$ equals _____.

Key: (54)

Exp: $E(X) = 5 \Rightarrow E(X^2) = 30$, where $X \sim P(\lambda), \lambda = 5$

$\therefore E[(X+2)^2] = E(X^2) + 4E(X) + 4$
 $= 30 + 20 + 4 = 54$

□

$(\because V(X) = E(X^2) - (E(X))^2)$

38. Consider the following C function

```
int fun (int n) {
    int i, j;
    for (i = 1; i <= n; i++) {
        for (j = 1; j < n; j+=i) {
            printf ("%d %d", i, j);
        }
    }
}
```

Time complexity of fun in terms of θ notation is

- (A) $\theta(n\sqrt{n})$ (B) $\theta(n^2)$ (C) $\theta(n \log n)$ (D) $\theta(n^2 \log n)$

Key: (C)

Exp: for $i = 1$

j will run from 1 to n by incrementing by '1' in each step \Rightarrow ' j ' will run for n times

For $i = 2$

j will run from 1 to n by incrementing by '2' in each step \Rightarrow j will run for $\frac{n}{2}$ times and so on

$$\begin{aligned} \text{Time Complexity (Tc)} &= n + \frac{n}{2} + \frac{n}{3} + \dots + \frac{n}{n} \\ &= n \left(1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{n} \right) = \theta(n \log n) \end{aligned}$$

39. The pre-order transversal of a binary search tree is given by 12, 8, 6, 2, 7, 9, 10, 16, 15, 19, 17, 20. Then the post-order traversal of this tree is:

- (A) 2,6,7,8,9,10,12,15,16,17,19,20 (B) 2,7,6,10,9,8,15,17,20,19,16,12
 (C) 7,2,6,8,9,10,20,17,19,15,16,12 (D) 7,6,2,10,9,8,15,16,17,20,19,12

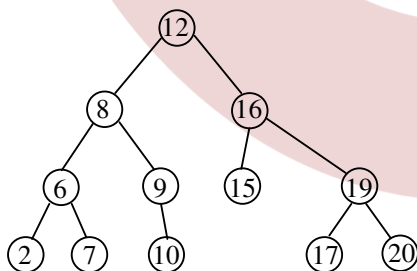
Key: (B)

Exp: Given: Preorder ! 12, 8, 6, 2, 7, 9, 10, 16, 15, 19, 17, 20

In order! 2, 6, 7, 8, 9, 10, 12, 15, 16, 17, 19, 20

Note: BST In order will give ascending order

Corresponding BST is



\therefore Post order is 2, 7, 6, 10, 9, 8, 15, 17, 20, 19, 16, 12

□

40. Consider the C program fragment below which is meant to divide x by y using repeated subtractions. The variables x , y , q and r are all unsigned int.

```
while (r >= y) {
    r = r - y;
    q = q + 1;
}
```

Which of the following conditions on the variables x , y , q and r before the execution of the fragment will ensure that the loop terminates in a state satisfying the condition $x == (y * q + r)$?

- (A) $(q == r) \ \&\& \ (r == 0)$
 (B) $(x > 0) \ \&\& \ (r == x) \ \&\& \ (y > 0)$
 (C) $(q == 0) \ \&\& \ (r == x) \ \&\& \ (y > 0)$
 (D) $(q == 0) \ \&\& \ (y > 0)$

Key: (C)

Exp: Given, program is:

```
while (r >= y){
    r = r - y;
    q = q + 1;
}
```

If we want final value as $x == (y * q + r)$. Then initial value of r should be equal to x (Since y is subtracted from r each time in given code). q incremented by 1 (q is quotient here). To avoid undefined behavior, value of y should be greater than zero.

Therefore, $(q == 0) \ \&\& \ (r == x) \ \&\& \ (y > 0)$

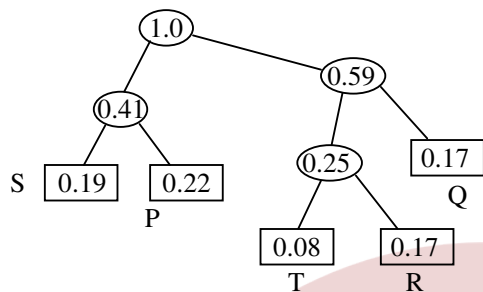
41. A message is made up entirely of characters from the set $X = \{P, Q, R, S, T\}$. The table of probabilities for each of the characters is shown below:

| Character | Probability |
|--------------|-------------|
| P | 0.22 |
| Q | 0.34 |
| R | 0.17 |
| S | 0.19 |
| T | 0.08 |
| Total | 1.00 |

If a message of 100 characters over X is encoded using Huffman coding, then the expected length of the encoded message in bits is _____ □

Key: (225)

Exp: Huffman tree is as follows



Average length of the character
 $= 2(0.19 + 0.22) + 2(0.34) + 3(0.08 + 0.17)$
 $= 2(0.41) + 2(0.34) + 3(0.25)$
 $= 0.82 + 0.68 + 0.75$
 $= 2.25 \text{ bits}$
 $\therefore \text{Message length} = 100 \times 2.25 \text{ bits} = 225 \text{ bits}$

42. The next state table of a 2-bit saturating up-counter is given below.

| Q_1 | Q_0 | Q_1^+ | Q_0^+ |
|-------|-------|---------|---------|
| 0 | 0 | 0 | 1 |
| 0 | 1 | 1 | 0 |
| 1 | 0 | 1 | 1 |
| 1 | 1 | 1 | 1 |

The counter is built as a synchronous sequential circuit using T flip-flops. The expression for T_1 and T_0 are

- (A) $T_1 = Q_1 Q_0, \quad T_0 = \overline{Q_1} \overline{Q_0}$
- (B) $T_1 = \overline{Q_1} Q_0, \quad T_0 = \overline{Q_1} + \overline{Q_0}$
- (C) $T_1 = Q_1 + Q_0, \quad T_0 = \overline{Q_1} + \overline{Q_0}$
- (D) $T_1 = Q_1 Q_0, \quad T_0 = \overline{Q_1} + \overline{Q_0}$

Key: (B)

Exp:

| Q_1 | Q_0 | Q_1^+ | Q_0^+ | T_1 | T_0 |
|-------|-------|---------|---------|-------|-------|
| 0 | 0 | 0 | 1 | 0 | 1 |
| 0 | 1 | 1 | 0 | 1 | 1 |
| 1 | 0 | 1 | 1 | 0 | 1 |
| 1 | 1 | 1 | 1 | 0 | 0 |

$$T_1 = \overline{Q_1} Q_0$$

$$T_0 = \overline{Q_1} + \overline{Q_0}$$

□

43. Consider the set of processes with arrival time (in milliseconds). CPU burst time (in milliseconds), and priority (0 is the highest priority) shown below. None of the processes have I/O burst time.

| Process | Arrival Time | Burst Time | Priority |
|----------------|--------------|------------|----------|
| P ₁ | 0 | 11 | 2 |
| P ₂ | 5 | 28 | 0 |
| P ₃ | 12 | 2 | 3 |
| P ₄ | 2 | 10 | 1 |
| P ₅ | 9 | 16 | 4 |

The average waiting time (in milliseconds) of all the processes using preemptive priority scheduling algorithm is _____

Key: (29)

Exp:

| PID | AT | BT | Priority | CT | TAT | Waiting Time |
|----------------|----|----|----------|----|-----|--------------|
| P ₁ | 0 | 11 | 2 | 49 | 49 | 38 |
| P ₂ | 5 | 28 | 0 | 33 | 28 | 0 |
| P ₃ | 12 | 2 | 3 | 51 | 39 | 37 |
| P ₄ | 2 | 10 | 1 | 40 | 38 | 28 |
| P ₅ | 9 | 16 | 4 | 67 | 58 | 42 |

Gantt Chart:

| | | | | | | |
|----------------|----------------|----------------|----------------|----------------|----------------|----------------|
| P ₁ | P ₄ | P ₂ | P ₄ | P ₁ | P ₃ | P ₅ |
| 0 | 2 | 5 | 33 | 40 | 49 | 51 |
| | | | | | | 67 |

Therefore Average waiting time = $\frac{(38 + 0 + 37 + 28 + 42)}{5} = \frac{145}{5} = 29$ ms

44. For any discrete random variable X, with probability mass function

$P(X = j) = p_j, p_j \geq 0, j \in \{0, \dots, N\}$ and $\sum_{j=0}^N p_j = 1$, define the polynomial function

$g_x(z) = \sum_{j=0}^N p_j z^j$ For a certain discrete random variable Y, there exists a scalar $\beta \in [0, 1]$ such

that $g_y(z) = (1 - \beta + \beta z)^N$. The expectation of Y is

- (A) $N\beta(1 - \beta)$
- (B) $N\beta$
- (C) $N(1 - \beta)$
- (D) Not expressible in terms of N and β alone

□

Key: (B)

45. The read access times and the hit ratios for different caches in a memory hierarchy are as given below.

| Cache | Read access time (in nanoseconds) | Hit ratio |
|----------|--------------------------------------|-----------|
| I-cache | 2 | 0.8 |
| D-cache | 2 | 0.9 |
| L2-cache | 8 | 0.9 |

The read access time of main memory is 90 nanoseconds. Assume that the caches use the referred word-first read policy and the write back policy. Assume that all the caches are direct mapped caches. Assume that the dirty bit is always 0 for all the blocks in the caches. In execution of a program, 60% of memory reads are for instruction fetch and 40% are for memory operand fetch. The average read access time in nanoseconds (up to 2 decimal places) is _____.

Key: (4.72)

Exp: Given,

| Cache | I-Cache | D-Cache | L ₂ -Cache | Main Memory |
|-----------------------------|---------|---------|-----------------------|-------------|
| Read Access Time (in ns) | 2 | 2 | 8 | 90 |
| Hit Ratio | 0.8 | 0.9 | 0.9 | 1.0 |

And in execution of program 60% of memory reads are for instruction fetch and 40% are for memory operand fetch.

Now,

Average instruction fetch time = I-cache access time + I-cache miss ratio * L₂-cache access time + I-cache miss rate * L₂-cache miss ratio * main memory access time
 $= 2 + (1 - 0.8) \times 8 + (1 - 0.8) \times (1 - 0.9) \times 90 = 5.4n \text{ sec}$

And average data fetch time = D-cache access time + D-cache miss ratio * L₂-cache access time + D-cache miss ratio * L₂-cache miss ratio * main memory access time
 $2 + (1 - 0.9) \times 8 + (1 - 0.9) \times (1 - 0.9) \times 90 = 3.7n \text{ sec}$

Therefore, average memory access time = Fraction of instruction fetch * average instruction fetch time + fraction of data fetch * Average data fetch time
 $= 0.6 \times 5.4 + 0.4 \times 3.7 = 4.72 \text{ (in n sec)}$

46. If the ordinary generating function of a sequence $\{a_n\}_{n=0}^{\infty}$ is $\frac{1+z}{(1-z)^3}$, then $a_3 - a_0$ is equal to _____.

Key: (15)

Exp: $f(z) = \frac{1}{1-z} = 1 + z + z^2 + \dots$

□

$$f'(z) = \frac{1}{(1-z)^2} = 1 + 2z + 3z^2 + \dots$$

$$\text{Consider } \frac{1+z}{(1-z)^3} = \frac{1}{(1-z)^2} + \frac{2z}{(1-z)^3}$$

$$\frac{1}{(1-z)^2} = 1 + 2z + 3z^2 + 4z^3 \dots$$

$$f''(z) = \frac{2}{(1-z)^3} = 2 + 6z + 12z^2 \dots$$

$$\frac{1}{(1-z)^2} + \frac{2z}{(1-z)^3} = (1 + 2z + 3z^2 + 4z^3 - \dots) + (2z + 6z^2 + 12z^3 \dots)$$

$$= 1 + 4z + 9z^2 + 16z^3 \dots$$

$$= a_0 + a_1z + a_2z^2 + a_3z^3 \dots$$

$$a_0 = 1$$

$$a_3 = 16$$

$$a_3 - a_0 = 16 - 1 = 15$$

47. Consider the following snippet of a C program. Assume that swap (&x, &y) exchanges the contents of x and y.

```
int main ( ) {
int array[]={3,5,1,4,6,2};
int done =0 ;
int i ;
while (done == 0) {
    done = 1;
    for (i = 0; i <=4; i++) {
        if (array [i] < array [i+1]) {
            swap (& array [i], &array [i+1]);
            done = 0;
        }
    }
}
for (i = 5 ; i > =1; i --)
if (array [i] > array [ i-1])
    swap ( & array [i] , &array [i-1]);
done = 0;
```

□

```
printf ( “ %d “ , array [3] );
```

The output of the program is _____.

Key: (3)

Exp: The final contents of the array is

| | | | | | |
|---|---|---|---|---|---|
| 6 | 5 | 4 | 3 | 2 | 1 |
|---|---|---|---|---|---|

∴ a[3]=3 will be printed

48. Consider the following C program.

```
# include <stdio.h>
```

```
int main ( )
```

```
int m = 10;
int n, n1;
n = ++m;
n1 = m++;
n--;
--n1;
n - = n1;
printf (“%d”, n) ;
return 0;
```

The output of the program is _____.

Key: (0)

Exp: m= 10

n = ++ m will increment m & assign it to n ⇒ n=11 & m =1

n₁ = m ++ will assign m to n₁ and then increment m by 1

⇒ n₁ =11, m=12

n --; decrement n by 1 ⇒ n =10

-- n₁; decrement n₁ by 1 ⇒ n₁ =10

n -= n₁; [same as n = n - n =10 - 10 = 0]

∴ '0' is printed

49. Consider the following database table named *top_scorer*.

top_scorer.

| Player | Country | Goals |
|----------|---------|-------|
| Klose | Germany | 16 |
| Ronald | Brazil | 15 |
| G Muller | Germany | 14 |

□

| | | |
|-----------|-----------|----|
| Fontaine | France | 13 |
| Pele | Brazil | 12 |
| Klinsmann | Germany | 11 |
| Kocsis | Hungary | 11 |
| Batistuta | Argentina | 10 |
| Cubillas | Peru | 10 |
| Lato | Poland | 10 |
| Lineker | England | 10 |
| T Miller | Germany | 10 |
| Rahn | Germany | 10 |

Consider the following SQL query:

```
SELECT ta.player FROM top_scorer AS ta
WHERE ta.goals > ALL (SELECT tb.goals
                     FROM top_scorer AS tb
                     WHERE tb.country = 'Spain')
AND ta.goals > ANY ( SELECT tc.goals
                    FROM top_scorer AS tc
                    WHERE tc.country = 'Germany')
```

The number of tuples returned by the above SQL query is _____.

Key: (7)

Exp: Player

- Klose
- Ronaldo
- G Muller
- Fontaine
- Pele
- Klinsmann
- Kocsis

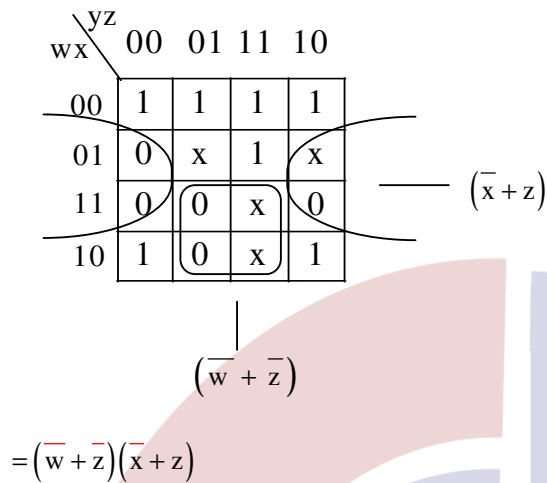
50. Given $f(w,x,y,z) = \sum_m (0,1,2,3,7,8,10) + \sum_d (5,6,11,15)$, where d represents the don't care condition in Karnaugh maps. Which of the following is a minimum product-of-sums (POS) form of $f(w,x,y,z)$?

- (A) $f = (\bar{w} + \bar{z})(\bar{x} + z)$
- (B) $f = (\bar{w} + z)(x + z)$
- (C) $f = (w + z)(\bar{x} + z)$
- (D) $f = (w + \bar{z})(\bar{x} + z)$

Key: (A)

Exp:

□



51. In a B⁺ tree, if the search –key value is 8 bytes long, the block size is 512 bytes and the block pointer size is 2 bytes, then maximum order of the B⁺ tree is _____.

Key: (52)

Exp: Let 'K' be the order
 $K(2) + (K - 1)(8) \leq 512$
 $\Rightarrow 2K + 8k - 8 \leq 512$
 $\Rightarrow 10K \leq 520 \Rightarrow K \leq \frac{520}{10}$
 $\therefore K \leq 52$

52. Let L(R) be the language represented by regular expression R. Let L(G) be the language generated by a context free grammar G. Let L(M) be the language accepted by a Turing machine M. Which of the following decision problems are undecidable ?

- I. Given a regular expression R and a string w, is $w \in L(R)$?
- II. Given a context-free grammar G, $L(G) = \emptyset$?
- III. Given a context-free grammar G, is $L(G) = \Sigma^*$ for some alphabet Σ ?
- IV. Given a Turing machine M and a string w, is $w \in L(M)$?

(A) I and IV only (B) II and III only (C) II, III and IV only (D) III and IV only

Key: (D)

Exp: L(R) is the language represented by regular expression
 L(G) is the language generated by context free grammar
 L(M) is the language accepted by Turing Machine

- I. The problem a given regular expression R and a string w, is $w \in L(R)$? , is a membership problem. Membership problem is decidable for Finite state machine and regular expression. □
- II. Given Context free grammar G, is $L(G) = \emptyset$? , is emptiness problem for context free grammar. Emptiness problem is decidable for CFG by checking usefulness of start symbol.

- III. A given context free grammar G , is $L(G)$ is Σ^* for some alphabet Σ ?, is undecidable problem. We can't check whether $L(G) = \Sigma^*$ or not but rather we can check complement of $L(G)$ is ϕ . Since context free language are not closed under complement operation $\overline{L(G)}$ may be language accepted by Turing Machine and we can't check emptiness for Turing machine.
- IV. Given a Turing Machine M and a string w , is $w \in L(M)$?, is a membership problem for TM. Membership problem is not a decidable problem for TM.

53. Consider a machine with a byte addressable main memory of 2^{32} bytes divided into blocks of size 32 bytes. Assume that a direct mapped cache having 512 cache lines is used with this machine. The size of the tag field in bits is _____.

Key: (18)

Exp:

$$32 - (5 + 9) = 18$$

\downarrow \downarrow \swarrow
 Total block block
 size identifier

54. Let δ denote that transition function and $\hat{\delta}$ denote the extended transition function of the ϵ -NFA whose transition table is given below:

| δ | ϵ | a | b |
|-------------------|-------------|-------------|-------------|
| $\rightarrow q_0$ | $\{q_2\}$ | $\{q_1\}$ | $\{q_0\}$ |
| q_1 | $\{q_2\}$ | $\{q_2\}$ | $\{q_3\}$ |
| q_2 | $\{q_0\}$ | \emptyset | \emptyset |
| q_3 | \emptyset | \emptyset | $\{q_2\}$ |

Then $\hat{\delta}(q_2, aba)$ is

- (A) \emptyset (B) $\{q_0, q_1, q_3\}$ (C) $\{q_0, q_1, q_2\}$ (D) $\{q_0, q_2, q_3\}$

Key: (C)

Exp:

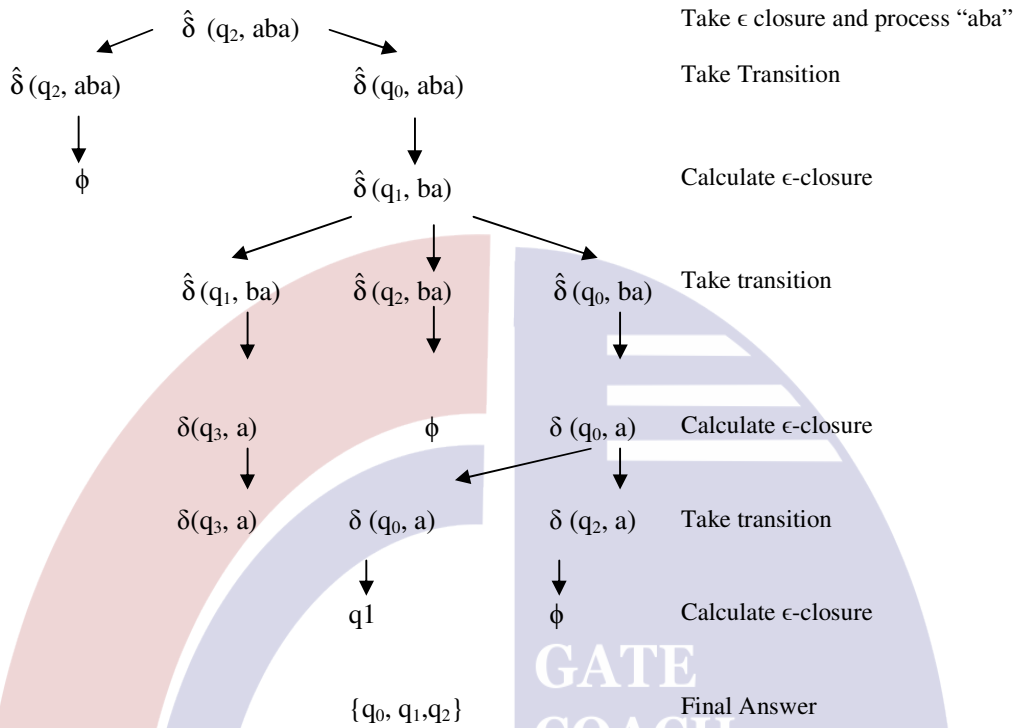
The given table for NFA- ϵ Transition is

| δ | ϵ | a | b |
|-------------------|------------|-----------|-----------|
| $\rightarrow q_0$ | $\{q_2\}$ | $\{q_1\}$ | $\{q_0\}$ |
| q_1 | $\{q_2\}$ | $\{q_2\}$ | $\{q_3\}$ |
| q_2 | $\{q_0\}$ | Φ | Φ |
| q_3 | Φ | Φ | $\{q_2\}$ |

□

The process is we start with ϵ -closure of q_2 then for each input first take the transition then calculate ϵ -closure

q_2 is the start for processing we take ϵ -closure which is $\{q_0, q_2\}$ and process "aba"



55. Consider the following languages.

$$L_1 = \{a^p \mid p \text{ is a prime number}\}$$

$$L_2 = \{a^n b^m c^{2m} \mid n \geq 0, m \geq 0\}$$

$$L_3 = \{a^n b^n c^{2n} \mid n \geq 0\}$$

$$L_4 = \{a^n b^n \mid n \geq 1\}$$

Which of the following are CORRECT ?

- I. L_1 is context-free but not regular.
- II. L_2 is not context-free.
- III. L_3 is not context-free but recursive.
- IV. L_4 is deterministic context-free.

(A) I, II and IV only (B) II and III only (C) I and IV only (D) III and IV only

Key: (D)

Exp: The given languages are

$$L_1 = \{a^p \mid p \text{ is a prime number}\}$$

$$L_2 = \{a^n b^m c^{2m} \mid n \geq 0, m \geq 0\}$$

$$L_3 = \{a^n b^n c^{2n} \mid n \geq 0\}$$

$$L_4 = \{a^n b^n \mid n \geq 1\}$$

Statements are:

- I. L_1 is context free but not regular is **INCORRECT**, It required a Turing machine to accept L_1 .

□

II. L_2 is not context free is **INCORRECT**; the context free grammar is

$$S \rightarrow XY$$

$$X \rightarrow aX\epsilon$$

$$Y \rightarrow bYc\epsilon$$

III. L_3 is not context free but recursive is **CORRECT**. L_3 is standard context sensitive language.

IV. L_4 is deterministic context free is **CORRECT**; the grammar is

$$S \rightarrow aSblab$$

General Aptitude

Q. No. 1 - 5 Carry One Mark Each

1. There are 3 red socks, 4 green socks and 3 blue socks, you choose 2 socks. The probability that they are of the same colour is _____.

- (A) 1/5 (B) 7/30 (C) 1/4 (D) 4/15

Key: (D)

Exp: Required probability = $\frac{3C_2 + 4C_2 + 3C_2}{10C_2} = \frac{4}{15}$

2. Choose the option with words that are not synonyms.

- (A) aversion, dislike (B) luminous, radiant
(C) plunder, loot (D) yielding, resistant

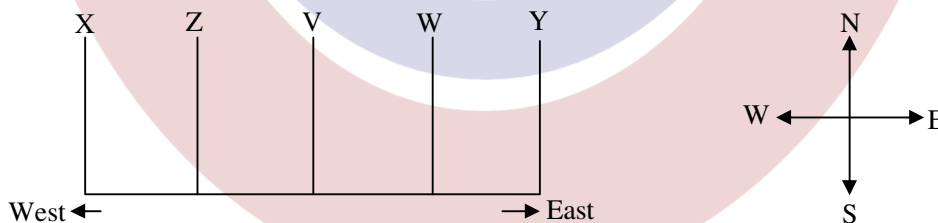
Key: (D)

3. There are five buildings called V, W, X, Y and Z in a row (not necessarily in that order). V is to the west of W. Z is to the East of X and the West of V. W is to the West of Y. Which is the building in the middle ?

- (A) V (B) W (C) X (D) Y

Key: (A)

Exp: From the given data, the following is formed



∴ The building 'V' is in the middle

4. A test has twenty questions worth 100 marks in total. There are two types of questions, multiple choice questions are worth 3 marks each and essay questions are worth 11 marks each. How many multiple choice questions does the exam have? □

- (A) 12 (B) 15 (C) 18 (D) 19

Key: (B)

Exp: $x + y = 20$ ($x = \text{MCQ}, y = \text{Essay type}$)

$$3x + 11y = 100$$

$$\Rightarrow x = 15, y = 5$$

5. Saturn is ____ to be seen on a clear night with the naked eye.

(A) enough bright

(B) bright enough

(C) as enough bright

(D) bright as enough

Key: (B)

Q. No. 6 – 10 Carry Two Marks Each

6. "We lived in a culture that denied any merit to literary works, considering them important only when they were handmaidens to something seemingly more urgent - namely ideology. This was a country where all gestures, even the most private, were interpreted in political terms."

The author's belief that ideology is not as important as literature is revealed by the word:

(A) 'culture'

(B) 'seemingly'

(C) 'urgent'

(D) 'political'

Key: (B)

7. X is a 30 digit number starting with the digit 4 followed by the digit 7, then the number X^3 will have

(A) 90 digits

(B) 91 digits

(C) 92 digits

(D) 93 digits

Key: (A)

Exp: $X = (47\text{.....})_{30 \text{ digits}}$

Suppose $(47)_{30 \text{ digits}}^3 = (2 + 2 + 2)$ digits in $(47)^3$

Similarly $(47)_{30 \text{ digits}}^3 =$ contains $(30 + 30 + 30)$ digits = 90 digits.

8. There are three boxes, one contains apples, another contains oranges and the last one contains both apples and oranges. All three are known to be incorrectly labelled. If you are permitted to open just one box and then pull out and inspect only one fruit, which box would you open to determine the contents of all three boxes?

(A) The box labelled 'Apples'

(B) The box labelled 'Apples and Oranges'

(C) The box labelled 'Oranges'

(D) Cannot be determined

Key: (B)

Exp: The person who is opening the boxes, he knew that all 3 are marked wrong.

Suppose if 3 boxes are labelled as below. □



(1) Apples



(2) Oranges



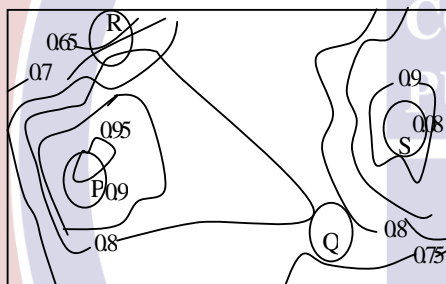
(3) Apples & Oranges

If he inspected from Box(1), picked one fruit, found orange, then he don't know whether box contains oranges (or) both apples and oranges.

Similarly, if he picked one fruit from box(2), found apple then he don't know whether box contain apples (or) both apples and oranges.

But if he picked one fruit from box(3), i.e., labelled is "apples and oranges", if he found apple then he can decide compulsorily that box(3) contains apples and as he knew all boxes are labelled as incorrect, he can tell box(2) contains both apples and oranges, box(1) contain remaining oranges. So, he should open box labelled 'Apples and Oranges' to determine contents of all the three boxes.

9. An air pressure contour line joins locations in a region having the same atmospheric pressure . The following is an air contour plot of a geographical region . Contour lines are shown at 0.05 bar intervals in this plot.



If the possibility of a thunderstorm is given by how fast air pressure rises or drops over a region, which of the following regions is most likely to have a thunderstorm?

- (A) P (B) Q (C) R (D) S

Key: (C)

Exp:

| Region | Air pressure difference |
|--------|-------------------------|
| P | $0.95 - 0.90 = 0.05$ |
| Q | $0.80 - 0.75 = 0.05$ |
| R | $0.85 - 0.65 = 0.20$ |
| S | $0.95 - 0.90 = 0.05$ |

In general thunder storms are occurred in a region where suddenly air pressure changes (i.e.,) sudden rise (or) sudden fall of air pressure. From the given contour map in 'R' region only more changes in air pressure. So, the possibility of a thunder storms in this region.

So option (C) is correct.

10. The number of roots of $e^x + 0.5x^2 - 2 = 0$ in the range $[-5, 5]$ is
(A) 0 (B) 1 (C) 2 (D) 3

Key: (A)

Exp: $f(x) = e^x + 0.5x^2 - 2$

$$f(-5) = 10.50; f(-4) = 6.01, f(-2) = 0.135; f(-1) = -1.13;$$

$$f(0) = -1, f(1) = 1.21, f(2) = 7.38, f(3), f(4), f(5) \text{ also } +ve.$$

\therefore As there are 2 sign changes from +ve to -ve and -ve to +ve, two roots will be there in the range $[-5, 5]$.



□